## Verification of Real-Time Systems Static WCET Analysis

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What does the execution time of a program depend on?

### Input-dependent control flow



### Microarchitectural State



### Formalization of WCET Analysis Problem



Measuring the execution time for all inputs and all hardware states is not feasible in practice:

- There are too many.
- We cannot control the initial hardware states.
- → Need for approximation!

 High-level Requirements for WCET Analysis

- Upper bounds must be safe, i.e. not underestimated.
- Upper bounds should be tight, i.e. not far away from real execution times.
- Analysis effort must be tolerable.

 Standard WCET Analysis Approach Today: Divide and Conquer + Abstraction

- 1. Divide: split program into fragments (e.g. basic blocks).
- W = 2 $\int e^{2\pi i t}$  Determine safe bounds on execution time of each fragment using abstractions.

3. Determine constraints on control flow (e.g. New loop bounds) through program by abstractions.

4. Conquer: combine 2 + 3 into bound of execution time of the whole program.





### Running Example





### Value Analysis

Determines invariants on values of registers at different program points. Invariants are often in the form of enclosing intervals of all possible values.

Where is this information used?

- Microarchitectural Analysis
  - Pipeline Analysis
  - Cache Analysis
- Control-Flow Analysis
  - Detect infeasible paths
  - Derive loop bounds









## Microarchitectural Analysis

Ideal 1970s world: one instruction = one cycle Real world:

- Pipelining
- Branch prediction + speculative execution
- Caches
- DRAM
- Execution time of individual instruction highly variable and dependent on state of microarchitecture
- Need to determine in which states the microarchitecture may be at a point in the program

# Pipelining

- Instruction execution is split into several stages
- Several instructions can be executed in parallel
- Some pipelines can start more than one instruction per cycle: VLIW, Superscalar
- Some processors can execute instructions <u>out</u>of-order
- Practical Problems: Hazards and cache misses

Fetch
Decode
Execute
WB



# Pipeline Hazards

Pipeline Hazards:

- Data Hazards: Operands not yet available (Data Dependences)
- Resource Hazards: Consecutive instructions use same resource
- Control Hazards: Conditional branch
- Instruction-Cache Hazards: Instruction fetch causes cache miss
  - · DATA CALIN

Assuming worst case everywhere is not an option!



## View of Processor as a State Machine

- Processor (pipeline, cache, memory, inputs) viewed as a *big* state machine, performing transitions every clock cycle
- Starting in an initial state for an instruction, transitions are performed, until a final state is reached:
  - End state: instruction has left the pipeline
  - # transitions: execution time of instruction

# A Concrete Pipeline Executing a Basic Block

## function exec (b : basic block, s : concrete pipeline state) t: trace

interprets instruction stream of *b* starting in state *s* producing trace *t*.

Successor basic block is interpreted starting in initial state *last(t)* 

*length(t)* gives number of cycles for basic block *b* 

# An Abstract Pipeline Executing a Basic Block

#### function <u>exec</u> (*b* : basic block, <u>s</u> : abstract pipeline state) <u>t</u>: trace

interprets instruction stream of b (annotated with cache information) starting in state <u>s</u> producing abstract trace <u>t</u> length(<u>t</u>) gives number of cycles

### • • • What is different?

- Abstract states may lack information, e.g. about cache contents.
- More than one trace may be possible.
- Starting state for successor basic block? In particular, if there are several predecessor blocks.



Alternatives:

- sets of states
- combine by least upper bound (join), hard to find one that
  - preserves information and
  - has a compact representation.



- In the concrete pipeline model, one state resulted in one new state after a one-cycle transition
- Now, in the abstract model, one state can have several successor states
  - Transitions from set of states to set of states

### Non-Locality of Local Contributions

- Interference between processor components produces Timing Anomalies:
  - Assuming local best case leads to higher overall execution time.
  - Assuming local worst case leads to shorter overall execution time
     Ex.: Cache miss in the context of branch prediction
- o Treating components in isolation may be unsafe
- o Implicit assumptions are not always correct:
  - Cache miss is not always the worst case!
  - The empty cache is not always the worst-case start!

An Abstract Pipeline Executing a Basic Block

function analyze (b : basic block, S : analysis state) T: set

of trace

Analysis states  $= 2^{PS \times CS}$ 

<u>PS</u> = set of <u>abstract</u> pipeline states

<u>CS</u> = set of abstract cache states

 $S_3 = S_1 \cup S_2$ 

interprets instruction stream of *b* (annotated with cache information) starting in state <u>S</u> producing set of traces <u>T</u> *max(length(<u>T</u>))* - upper bound for execution time *last(<u>T</u>)* - set of initial states for successor block
Union for blocks with several predecessors.







- Determines a worst-case path and an upper bound on the WCET.
- o Formulated as integer linear program (ILP).





... + Restriction to integers = ILP.

### LP is in polynomial time, yet, ILP is NP hard, but often efficiently solvable in practice.

Solvers (e.g. CPLEX) determine the maximal value of the objective function + corresponding valuation of variables.



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### Global Bound Analysis aka Path Analysis aka Implicit Path Enumeration



Solution:

$$x_a = x_f = 1$$
,  $x_b = 43$ ,  $x_c = x_d = 42$   
Objective function = 2\*1 + 3\*43 + (6+3)\*42 + 2\*1 = 511

## Summary and Outlook

• Divide and conquer:

- Analyze worst-case timing of program fragments separately
- Combine results using integer linear program
- Abstraction:
  - Employ sound abstractions to solve undecidable problems approximately

Next week:

theoretical background of Abstract Interpretation